AMESA Office
P.O Box 54

WITS
2050
Tel: 0117173461
Fax: 0117173459
Cell: 0832924077
Email: president@amesa.org.za
Wepage: www.amesa.org.za
Facebook: www.facebook.com/amesa93
29 November 2012

Mr Bobby Soobrayan<br>Director General<br>Department of Basic Education<br>222 Struben Street<br>PRETORIA

## AMESA report on the 2012 Mathematics \& Mathematical Literacy Examination Papers

Dear Mr Soobrayan
On behalf of the National Council of the Association for Mathematics Education of South Africa (AMESA), I would like to commend the Department of Basic Education for the wonderful support afforded the Grade 12 learners and their teachers in the 2012 academic year.

As we have done for the past several years, I would like to make a formal submission of the AMESA Report on the 2012 Mathematics and Mathematical Literacy Examination Papers 1 and 2 that were written by the Grade 12 learners.

The purpose of the report is to provide constructive feedback to the Department in the spirit of promoting mathematics education and enhancing the quality of the teaching and learning of Mathematics in South Africa.

It is our hope that the report, especially the question by question analyses, will be useful to the examiners, markers and moderators in our attempt to promote the high standard of mathematics education in our country.

Sincerely


Alwyn Olivier
AMESA President

Association for Mathematics Education of South Africa

## INTRODUCTION

The 2012 Grade 12 papers for Mathematics and Mathematical Literacy were written on Friday 2 November 2012 (Paper 1) and Monday 5 November 2012 (Paper 2).

AMESA regions (provinces) throughout South Africa soon after embarked on a workshop activity to review these papers according to specific criteria and guidelines. The provinces submitted their reports to the AMESA National Curriculum Committee. This report was then compiled by the Curriculum Committee and represents a summary of the findings and trends of the AMESA provincial reports.

The report covers specific comments on each paper focusing on the following aspects:
A. Overall Review

1. Technical Aspects (typing, diagrams, etc.)
2. Language used and compliance with the cognitive levels of thinking
3. Curriculum coverage
4. Comparison with 2011 papers
5. Overall Observations
B. Question by Question Analysis

Participants were "trained" in the analysis of questions using the analysis tool at a workshop during AMESA's annual congress in Potchefstroom in June 2012. Although we do not claim any validity of the analysis, we are nevertheless confident that it represents a fairly balanced and accurate perspective from a cross-section of teachers throughout the country.

Association for Mathematics Education of South Africa

## MATHEMATICS PAPER 1

## A. OVERALL REVIEW

1. Technical aspects (typing, diagrams, etc.)

The paper was clear with no typing errors. The diagrams were well constructed, neat and clear.
The Department of Basic Education is to be complimented for its high technical standard.
2. Language used

The language used in the paper would be within the reach of most Grade 12 mathematics learners. Learners would have been familiar with the terms and concepts used in the paper. One area where there may have been confusion would be in question 7.1 where the term "diminishing-balance" rather than "reducing-balance" was used. However, this was not a serious issue as learners would have recognised the meaning of "diminishing" in this context.
3. Syllabus coverage

| Code | Content/Topic | Suggested | November 2012 |
| :---: | :--- | :---: | :---: |
| 1 | Patterns \& Sequences (LO1) | 30 | 31 |
| 2 | Annuities \& Finance (LO1) | 15 | 17 |
| 3 | Functions \& Graphs (LO2) | 35 | 33 |
| 4 | Algebraic manipulation; equations (LO2) | 20 | 21 |
| 5 | Calculus (LO2) | 35 | 34 |
| 6 | Linear Programming (LO2) | 15 | 14 |
|  | Total | $\mathbf{1 5 0}$ | $\mathbf{1 5 0}$ |

The above table gives a clear indication of the sections which appeared in the paper. These are in line with the prescriptions of the Subject Assessment Guidelines for Mathematics.

### 4.1 Standard of paper

The paper appeared to be a reasonable paper with a good spread of questions across ability levels.

### 4.2 Compliance with levels of thinking

| Code | Levels of thinking | Suggested | November 2012 |
| :---: | :--- | :---: | :---: |
| 1 | Knowledge | $\pm 25 \%$ | $22,7 \%$ |
| 2 | Routine procedures | $\pm 30 \%$ | $36 \%$ |
| 3 | Complex procedures | $\pm 30 \%$ | $26 \%$ |
| 4 | Solving problems | $\pm 15 \%$ | $15,3 \%$ |

The table above shows that the paper was well balanced and within the acceptable range for each level of thinking as prescribed by the Subject Assessment Guidelines.

## 5. Comparison with 2011 paper

The paper was similar in standard to the 2011 paper with a good alternation of testing concepts between 2011 and 2012. This ensured that the 2012 paper was "different" from the 2011 paper and was not easily predictable.

Learners were eased into the examination paper as question 1 this year was straight forward, thus, not putting learners off right from the start.

Certain questions also tested the understanding of concepts, rather than just normal procedures, for example, questions 1.3, 6, 8.3.2, 9.2.2, 9.3, 11.3.3
6. Overall verdict

It would appear to be a well-balanced, but cognitively demanding paper.

Association for Mathematics Education of South Africa

## B. QUESTION BY QUESTION ANALYSIS

| Quest. | Content | Levels |  |  |  | Marks | Topic | Comment |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 |  |  |  |
| Question 1: Algebraic manipulation - Equations and inequalities |  |  |  |  |  |  |  |  |
| 1.1.1 | Quad equation | 2 |  |  |  | 2 | 4 | Straight-forward |
| 1.1.2 | Quad equation | 2 | 2 |  |  | 4 |  | Use of formula |
| 1.1.3 | Quad inequality |  | 3 | 1 |  | 4 |  | Use number line or graph |
| 1.2.1 | Simultaneous equation | 2 | 2 | 2 |  | 6 |  | Solve for x in terms of y then substitute in $\mathrm{xy}=8$ |
| 1.2.2 | Reflection |  | 1 | 1 |  | 2 |  | Procedural |
| 1.3.1 | Equal solutions |  | 2 |  |  | 2 |  | Equating term under square root sign to zero |
| 1.3.2 | No real solutions |  | 1 |  |  | 1 |  | Term under square root sign must be less than zero |
| Total |  | 6 | 11 | 4 |  | 21 |  |  |

## Question 2: Patterns and sequences

| 2.1 | Arithmetic sequence | 1 | 1 |  |  | 2 |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| 2.2 .1 | Term of arithmetic <br> sequence | 1 | 1 |  |  | 2 |
| G.2.2 | Given $\mathrm{S}_{\mathrm{n}}$, calculate n | 1 | 2 | 3 |  | 6 |
| Total |  | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{3}$ |  | $\mathbf{1 0}$ |

1 Form appropriate equation and solve for x
Use of simultaneous equations
Forming a quadratic equation in n and solving

Question 3: Patterns and Sequences


Association for Mathematics Education of South Africa

| Quest. | Content | Levels |  |  |  | Marks | Topic | Comment |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 |  |  |  |
| Question 4: Functions and graphs (cont.) |  |  |  |  |  |  |  |  |
| 4.2.1 | Calculation of $y$ intercept |  |  | 2 |  | 2 |  | y-intercept of straight line; not obvious |
| 4.2.2 | Equation of parabola |  | 2 | 2 |  | 4 |  | Applying x-intercepts and using d's value from 4.2.1 |
| 4.2.3 | Turning point of parabola |  | 2 |  |  | 2 |  | Routine procedure to calculate turning point |
| 4.2.4 | Two distinct roots |  |  |  | 2 | 2 |  | Interpreting parabola and a line parallel to x-axis which cuts parabola at two points |
| 4.2.5 | Maximum value of compound function |  |  | 2 | 1 | 3 |  | Finding the maximum value of $\mathrm{f}(\mathrm{x})$ and then $\mathrm{h}(\mathrm{x})$ |
| Total |  | 4 | 7 | 6 | 3 | 20 |  |  |

Question 5: Functions and Graphs

| 5.1 | Solve graph inequality |  | 2 |  |  | 2 |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| 5.2 | Inverse | 1 | 1 | 1 |  | 3 |
| 5.3 | Sketch of inverse | 1 | 2 |  |  | 3 |
| 5.4 | Transformation | 1 |  |  |  | 1 |
| Total |  | $\mathbf{3}$ | $\mathbf{5}$ | $\mathbf{1}$ |  | $\mathbf{9}$ |

3 Use graph to find out when graph is above line $y=-9$
Calculating inverse
Sketching inverse and showing some points
Describing a given transformation

Question 6: Functions and Graphs

| Total | Determining equation <br> of hyperbola |  | $\mathbf{2}$ | $\mathbf{2}$ | $\mathbf{4}$ | $\mathbf{3}$ | Using given information to obtain <br> equation of hyperbola; no <br> obvious route |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Question 7: Annuities and Finance

| 7.1.1 | Scrap value | 2 | 1 |  |  | 3 |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| 7.1 .2 | Cost of new machine | 1 | 2 |  |  | 3 |
| 7.1 .3 | Sinking fund |  | 1 | 2 | 2 | 5 |
| 7.2 | Compound investment; <br> determining number of <br> months | 1 | 1 | 2 | 2 | 6 |
| Total |  | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{4}$ | $\mathbf{4}$ | $\mathbf{1 7}$ |

Question 8: Calculus

| 8.1 | First principles | 2 | 3 |  |  | 5 | 5 | Finding derivative from first principles |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 8.2 | Using rules to differentiate | 1 | 2 |  |  | 3 |  | Using rules; different notation |
| 8.3.1 | Divide then differentiate |  | 1 | 1 |  | 2 |  | Derivative of a quotient; simplify first |
| 8.3.2 | Reasoning |  |  | 1 |  | 1 |  | $\mathrm{g}(1)$ is undefined |
| Total |  | 3 | 6 | 2 |  | 11 |  |  |
|  |  | 1 | 2 | 3 | 4 |  |  |  |
| Quest. | Content | Levels |  |  |  | Marks | Topic | Comment |

Association for Mathematics Education of South Africa

| Quest. | Content | Levels |  |  |  | Marks | Topic | Comment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | 1 | 2 | 3 | 4 |  |  |  |

## Question 9: Calculus

| 9.1.1 | x-coordinates of turning points cubic graph | 2 | 2 |  | 4 | 5 | Differentiate and solve for x |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 9.1.2 | $x$-coordinate of point where $f^{\prime}(x)$ is a maximum | 2 | 1 |  | 3 |  | Maximum value of derived function (quadratic) |
| 9.2.1 | Equation of tangent | 2 | 2 |  | 4 |  | Substitute $x=-1$ in derivative to obtain gradient; substitute $x=-1$ in function to get $y$ value; use gradient-point method |
| 9.2.2 | No point of intersection |  | 2 | 1 | 3 |  | Roots are not real |
| 9.3 | Reasoning |  |  | 3 | 3 |  | Derivative is always positive |
| Total |  | 6 | 7 | 4 | 17 |  |  |

Question 10: Calculus

| 10.1 | Initial velocity | 1 | 2 |  |  | 3 | 5 | Differentiate distance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10.2 | Rate of change of velocity | 1 |  |  |  | 1 |  | Differentiate velocity |
| 10.3 | Calculation of time |  | 1 | 1 |  | 2 |  | Calculate t when $\mathrm{s}(\mathrm{t})$ is a mininum |
| Total |  | 2 | 3 | 1 |  | 6 |  |  |
| Question 11: Linear programming |  |  |  |  |  |  |  |  |
| 11.1 | Interpreting graphs in linear programming |  |  | 1 |  | 1 | 6 | Check whether the point (15;5) lies in feasible region Formulating algebraic inequalities |
| 11.2 | Algebraic inequalities/ constraints | 2 | 2 | 2 |  | 6 |  |  |
| 11.3.1 | Maximum profit |  | 1 |  |  | 1 |  | Identifying the point which shows maximum profit |
| 11.3.2 | Profit from graph |  |  |  | 2 | 2 |  | Comparing profit |
| 11.3.3 | Maximum value of a quotient |  |  | 2 | 2 | 4 |  | Calculation of gradient |
| Total |  | 2 | 3 | 5 | 4 | 14 |  |  |


| Summary of marks and levels |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Question | $\mathbf{y}$ | Marks |  |  |  |
|  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |  |
| 1 | 6 | 11 | 4 |  | 21 |
| 2 | 3 | 4 | 3 |  | 10 |
| 3 | 7 | 4 | 4 | 6 | 21 |
| 4 | 4 | 7 | 6 | 3 | 20 |
| 5 | 3 | 5 | 1 |  | 9 |
| 6 |  |  | 2 | 2 | 4 |
| 7 | 4 | 5 | 4 | 4 | 17 |
| 8 | 3 | 6 | 2 |  | 11 |
| 9 |  | 6 | 7 | 4 | 17 |
| 10 | 2 | 3 | 1 |  | 6 |
| $\mathbf{1 1}$ | 2 | 3 | 5 | 4 | $\mathbf{1 4}$ |
| Total | $\mathbf{3 4}$ | $\mathbf{5 4}$ | $\mathbf{3 9}$ | $\mathbf{2 3}$ | $\mathbf{1 5 0}$ |
| Percentage | $\mathbf{2 2 , 7}$ | $\mathbf{3 6}$ | $\mathbf{2 6}$ | $\mathbf{1 5 , 3}$ | $\mathbf{1 0 0}$ |

Association for Mathematics Education of South Africa

## MATHEMATICS PAPER 2

## A. OVERALL REVIEW

1. Technical Aspects (typing, diagrams, etc)

As far as the technical criteria of compliance are concerned, the typing was clear and error free, diagrams were clear and understandable. In question 6, the point $K$ is not specified or described. However, most learners took $K$ as the $x$-intercept of the line $P Q$. It would have helped learners see the 3D in question 12 if the floor plane CBD was shaded.
2. Language used

The language usage was clear and understandable. It is expected that learners would have been familiar with the language used in the paper as they would have come across terms and concepts used in this paper in their school based assessment tasks and from previous papers. There were no terms or phrases that would have disadvantaged learners considerably.
3. Syllabus coverage

| Code | Content/Topic | Suggested | November 2012 |
| :---: | :--- | :---: | :---: |
| 1 | Coordinate Geometry | 40 | 37 |
| 2 | Transformation Geometry | 25 | 23 |
| 3 | Trigonometry | 60 | 62 |
| 4 | Data Handling | 25 | 28 |
|  | Total | $\mathbf{1 5 0}$ | $\mathbf{1 5 0}$ |

### 4.1 Standard of paper

It was an excellent paper with a good balance between routine and higher order questions. There were some challenging questions but these could not be regarded as unfair.

### 4.2 Compliance with levels of thinking

| Code | Levels of thinking | Suggested | November 2012 |
| :---: | :--- | :---: | :---: |
| 1 | Knowledge | $\pm 25 \%$ | $22 \%$ |
| 2 | Routine procedures | $\pm 30 \%$ | $33,3 \%$ |
| 3 | Complex procedures | $\pm 30 \%$ | $30 \%$ |
| 4 | Solving problems | $\pm 15 \%$ | $14,7 \%$ |

The above table shows that the paper was well balanced and in line with the prescriptions of the Subject Assessment Guidelines for Mathematics.

## 5. Comparison with 2011 paper

Teachers commented that this paper was far superior to the 2011 paper. The examiners are to be commended for a thought-provoking, quality paper.

## 6. Overall verdict

The paper could be classified as a fair, well balanced paper. Learners who were well prepared should pass as there were enough" knowledge and "routine procedures" to enable learners to pass.

## B. QUESTION BY QUESTION ANALYSIS

| Quest. | Content | Levels |  |  |  | Marks | Topic | Comment |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 |  |  |  |
| Question 1: Data handling |  |  |  |  |  |  |  |  |
| 1.1 | Interpret scatter plot | 1 |  |  |  | 1 | 4 | Straight-forward |
| 1.2 | Analyse scatter plot |  | 1 |  |  | 1 |  | Describe trend |
| 1.3 | Reading off approximate values |  | 2 | 1 |  | 3 |  | Approximate increase |
| 1.4 | Reasoning |  |  |  | 1 | 1 |  | Knowing that one's height reaches a maximum value by age 18 and remains the same |
|  | TOTAL | 1 | 3 | 1 | 1 | 6 |  |  |

## Question 2: Data handling

| 2.1 | Average | 2 |  |  |  | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| 2.2 | Standard deviation |  | 2 |  |  | 2 |
| 2.3 | Adding data and effect <br> on standard deviation |  |  | 2 |  | 2 |
| 2.4 | Average | 1 |  | 2 |  | 3 |
|  | TOTAL | $\mathbf{3}$ | $\mathbf{2}$ | $\mathbf{4}$ |  | $\mathbf{9}$ |

4

Add and divide by 8
Simple use of calculator
Effect of performance with larger
data set
Average of last 5 games to influence overall average, no obvious route

Question 3: Data handling

| 3.1 | Interpret box-andwhisker diagram | 1 |  |  |  | 1 | 4 | Simple application |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.2 | Draw box-and-whisker diagram | 2 | 2 |  |  | 4 |  | Simple drawing |
| 3.3 | Interpret diagram drawn |  | 1 | 1 |  | 2 |  | Interpretation |
| 3.4 | Validity of claim |  |  |  | 2 | 2 |  | Justification of claim |
|  | TOTAL | 3 | 3 | 1 | 2 | 9 |  |  |

## Question 4: Data handling

| 4.1 | Modal class from ogive |  | 1 |  |  | 1 |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| 4.2 | Median weight from <br> ogive |  | 1 |  |  | 1 |
| 4.3 | Calculation from ogive | 1 | 1 |  |  | 2 |
|  | TOTAL | $\mathbf{1}$ | $\mathbf{3}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{4}$ |

4
Determining the highest frequency

Question 5: Coordinate geometry

| 5.1 | Midpoint of a rhombus |  | 2 |  |  | 2 | 1 | Simple calculation |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5.2 | Gradient of line BC | 1 | 1 |  |  | 2 |  | Gradient of BC = gradient of BE |
| 5.3 | Equation of line AD |  | 2 | 1 |  | 3 |  | Gradient of $A D=$ gradient of $B C$, use point -gradient |
| 5.4 | Calculate angle using gradient |  |  | 3 | 3 | 6 |  | High level, using two sets of gradients and properties of triangles and rhombus |
|  | TOTAL | 1 | 5 | 4 | 3 | 13 |  |  |
|  |  | 1 | 2 | 3 | 4 |  |  |  |
| Quest. | Content | Levels |  |  |  | Marks | Topic | Comment |

Association for Mathematics Education of South Africa

| Quest. | Content | Levels |  |  |  | Marks | Topic | Comment |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 |  |  |  |
| Question 6: Coordinate geometry |  |  |  |  |  |  |  |  |
| 6.1 | Radius $\perp_{\text {tangent }}$ | 1 |  |  |  | 1 |  | Known fact |
| 6.2 | Coordinate of point on x -axis | 1 |  |  |  | 1 | 1 | Simple procedure |
| 6.3 | Equation of circle | 1 | 2 |  |  | 3 |  | Know centre and radius NL |
| 6.4 | Length of KL |  | 1 | 2 |  | 3 |  | Find K and subtract |
| 6.5 | Equation of AB | 2 | 2 |  |  | 4 |  | Know gradient of PQ , use gradient-point method |
| 6.6 | Calculation of coordinates of A |  | 1 | 2 |  | 3 |  | Point of intersection |
| 6.7 | Length of KA |  | 1 | 2 |  | 3 |  | Use distance formula |
| 6.8 | Show KLNA is a kite |  | 1 |  | 1 | 2 |  | Properties of a kite |
| 6.9 | Show angle ABK $=45^{\circ}$ |  | 1 |  | 2 | 3 |  | Know KA and AB, use tan ratio |
| 6.10 | Coordinates of centre of new circle |  | 1 |  |  | 1 |  | Simple procedure |
|  | TOTAL | 5 | 10 | 6 | 3 | 24 |  |  |

Question 7: Transformation geometry

| 7.1 | Transformation |  | 1 | 1 |  | 2 |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| 7.2 | General rule | 1 | 1 |  |  | 2 |
| 7.3 | Drawing an enlargement |  | 2 |  |  | 2 |
| 7.4 | General rule | 1 |  |  |  | 1 |
| 7.5 .1 | Reflection |  | 1 | 1 |  | 2 |
| 7.5 .2 | General rule | 2 |  |  |  | 2 |
| 7.5 .3 | Transformation |  |  |  | 2 | 2 |
|  | TOTAL | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{2}$ | $\mathbf{2}$ | $\mathbf{1 3}$ |

2 Describing a single transformation (rotation)
Writing down the general rule
Drawing enlarged triangle
Writing down the general rule
Coordinates of image
Writing down the general rule
Describing a single transformation

Question 8: Trigonometry

| 8.1.1 | Value from diagram |  | 2 |  |  | 2 |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| 8.1 .2 | Value of $\cos \alpha$ | 1 |  |  |  | 1 |
| 8.1 .3 | Value of $\cos \beta$ | 2 |  |  |  | 2 |
| 8.1 .4 | Value of $\sin (\beta-\alpha)$ | 1 | 1 | 2 |  | 4 |
| 8.2 .1 | Proving an identity |  |  | 4 |  | 4 |
| 8.2 .2 |  | Solving trig equation | 1 | 2 | 1 |  |
|  | TOTAL | $\mathbf{5}$ | $\mathbf{5}$ | $\mathbf{7}$ | $\mathbf{0}$ | $\mathbf{1 7}$ |

$3 \quad$ Calculate k using theorem of Pythagoras
Simple procedure
Reduction, simple procedure
Application of compound angle
expansion
Using known identities to prove given identity
Simple trig equation

Question 9: Trigonometry

| 9.1 | Simplifying trig <br> Expression | 1 | 2 | 2 |  | 5 |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| 9.2 | Simplifying without <br> using a calculator | 2 | 2 | 2 | 2 | 8 |
|  | TOTAL | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{4}$ | $\mathbf{2}$ | $\mathbf{1 3}$ |

3 Different reductions and special angle
Rewriting angles in terms of suitable angles and simplify without a calculator

Question 10: Trigonometry

| 10.1 | Calculation from trig graphs | 1 |  |  |  | 1 | 3 | Substitute or read off and subtract |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10.2 | x-coordinates of points of intersection to be calculated |  |  | 5 | 2 | 7 |  | Solve trig equations |
| 10.3 | Interpreting graph inequality | 1 | 1 |  |  | ${ }^{2}$ |  | When is $f(x)$ above and equal to $g(x)$ ? |
| 10.4 | The relationship between two graphs |  |  | 2 |  | 2 |  | Describing a given relationship; solution not obvious |
|  | TOTAL | 2 | 1 | 7 | 2 | 12 |  |  |
|  |  | 1 | 2 | 3 | 4 |  |  |  |
| Quest. | Content | Levels |  |  |  | Marks | Topic | Comment |

Association for Mathematics Education of South Africa

| Quest. | Content | Levels |  |  | Marks | Topic | Comment |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | 1 | 2 | 3 | 4 |  |  |  |

## Question 11: Trigonometry

| 11.1 | Area of parallelogram | 1 | 2 |  |  | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| 11.2 | Given the area, <br> calculate $\theta$ | 1 | 2 |  |  | 3 |
| 11.3 | Area of parallelogram <br> is a maximum |  |  |  | 2 | 2 |
|  | Total | $\mathbf{2}$ | $\mathbf{4}$ |  | $\mathbf{2}$ | $\mathbf{8}$ |

3 Simple application Calculating an angle from the area formula
What angle will make $6 \sin \boldsymbol{\theta}$ a maximum?

## Question 12: Trigonometry

| 12.1 | Using trig rules to determine CB in terms of $k$ and $\sin x$ | 1 | 2 | 2 |  | 5 | 3 | Application of trig rules and identities |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12.2 | Length (of rope) | 1 |  | 2 |  | 3 |  | Use the cosine ratio |
| 12.3 | Calculate angle (between ropes) | 1 | 1 | 1 | 1 | 4 |  | Use of cosine rule |
|  | TOTAL | 3 | 3 | 5 | 1 | 12 |  |  |

Question 13: Transformation geometry/Trigonometry

| 13.1 | Calculate transformed <br> point (after rotation <br> through an angle <br> about the origin) |  |  | 4 | 2 | 6 | $\mathbf{2 / 3}$ | Rotation through an angle |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :--- |
| 13.2 | Calculate the angle <br> between OD and OD' |  | 2 |  | 2 | 4 |  | Difference between angle POD <br> and P'OD ${ }^{\prime}$ |
|  | TOTAL |  | $\mathbf{2}$ | $\mathbf{4}$ | $\mathbf{4}$ | $\mathbf{1 0}$ |  |  |


| Summary of marks and levels |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Question | Levels |  |  |  |  |  | Marks |
|  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |  |  |  |
| 1 | 1 | 3 | 1 | 1 | 6 |  |  |
| 2 | 3 | 2 | 4 | - | 9 |  |  |
| 3 | 3 | 3 | 1 | 2 | 9 |  |  |
| 4 | 1 | 3 | 0 | 0 | 4 |  |  |
| 5 | 1 | 5 | 4 | 3 | 13 |  |  |
| 6 | 5 | 10 | 6 | 3 | 24 |  |  |
| 7 | 4 | 5 | 2 | 2 | 13 |  |  |
| 8 | 5 | 5 | 7 | 0 | 17 |  |  |
| 9 | 3 | 4 | 4 | 2 | 13 |  |  |
| 10 | 2 | 1 | 7 | 2 | 12 |  |  |
| 11 | 2 | 4 | - | 2 | 8 |  |  |
| 12 | 3 | 3 | 5 | 1 | 12 |  |  |
| $\mathbf{1 3}$ |  | 2 | 4 | 4 | 10 |  |  |
| Total | $\mathbf{3 3}$ | $\mathbf{5 0}$ | $\mathbf{4 5}$ | $\mathbf{2 2}$ | $\mathbf{1 5 0}$ |  |  |
| Percentage | $\mathbf{2 2} \%$ | $\mathbf{3 3 , 3} \%$ | $\mathbf{3 0} \%$ | $\mathbf{1 4 , 7} \%$ | $\mathbf{1 0 0} \%$ |  |  |

Association for Mathematics Education of South Africa

## MATHEMATICAL LITERACY PAPER 1

## A. OVERALL REVIEW

1. Technical Aspects (typing, diagrams, etc.)

The technical aspects of the paper are in keeping with the high standard set by the Department of Basic Education. All diagrams, graphs, etc were clear and readable.
2. Language used

There was good use of language in the paper. The terminology used should have been familiar to most Mathematical Literacy learners. However, learners had to do a lot of reading before getting to the questions (questions 2.1; 2.4; 4.1; 5.2, 6).This would disadvantage $2^{\text {nd }}$ language learners. Some teachers described the paper as a "comprehension" test.
3. Syllabus coverage

| Code | Learning Outcomes | Suggested | November 2012 |
| :---: | :--- | :---: | :---: |
| LO1 | Numbers and operations in context | 37 | 34 |
| LO2 | Functional relationships | 38 | 36 |
| LO3 | Space, Shape and measurement | 38 | 39 |
| LO4 | Data Handling | 37 | 41 |
|  |  |  | $\mathbf{1 5 0}$ |
|  | Total | $\mathbf{1 5 0}$ |  |

The coverage of the paper in terms of the 4 learning outcomes was in keeping with the Subject Assessment Guidelines for Mathematical Literacy.

### 4.1 Standard of paper

The question paper was of a good and acceptable standard for Mathematical Literacy paper 1. The questions were set in such a way that it is easy to distinguish between the sub-sections. The questions ranged from very easy to slightly difficult. This is in keeping with the departmental requirement that only "knowledge" and "routine procedures" questions form part of Mathematical Literacy P1.
Teachers observed that too many marks were allocated to the following questions:
1.1.7;1.2;1.3.4;1.4.2;2.1.1;2.1.2;3.3.3;4.1.3;6.3.3;6.4.2(b)

### 4.2 Compliance with levels of thinking

| Code | Levels of thinking | Suggested | November 2012 |
| :---: | :--- | :---: | :---: |
| 1 | Knowledge | $\pm 25 \%$ | $56 \%$ |
| 2 | Routine procedures | $\pm 30 \%$ | $44 \%$ |
| 3 | Complex procedures | $\pm 30 \%$ | - |
| 4 | Solving problems | $\pm 15 \%$ | - |

According to the Subject Assessment Guidelines, Mathematical Literacy Paper 1, comprises of only "knowledge" and "routine procedures" questions. Our analysis of the paper revealed the above mark allocation which was within the prescribed guidelines.
5. Comparison with 2011 paper

The 2012 was set at a similar standard to the 2011 paper, but marginally more difficult when comparing the "knowledge" and "routine procedures" questions for both years.
Nonetheless, some teachers reported that learners were able to finish the paper within two hours.
6. Overall verdict

A very fair but "easy" paper, set at the appropriate Grade 12 standard. Learners (and teachers) cannot complain about this paper.

Association for Mathematics Education of South Africa

## B. QUESTION BY QUESTION ANALYSIS

| Quest. | Content | Levels |  |  | Marks | Topic | Comment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | 1 | 2 | 3 | 4 |  |  |

Question 1

| 1.1.1 | Number calculations | 2 |  |  |  | 2 | Easy calculations <br> Very easy |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.1.2 | Conversion of decimal to fraction | 2 |  |  |  | 2 |  |
| 1.1.3 | Conversion of units | 2 |  |  |  | 2 |  |
| 1.1.4 | Multiplication | 2 |  |  |  | 2 |  |
| 1.1.5 | Time calculations | 2 |  |  |  | 2 |  |
| 1.1.6 | Exchange rate | 2 |  |  |  | 2 | Division |
| 1.1.7 | Probability | 2 |  |  |  | 2 | 'Silly' question! |
| 1.1.8 | Median | 2 |  |  |  | 2 | Some learners may struggle with three rows of data from a reading perspective |
| 1.2 | Reading off bar graph | 3 |  |  |  | 3 | May be difficult to read |
| 1.3.1 | Multiplication | 2 |  |  |  | 2 | Easy |
| 1.3.2 | Division | 2 |  |  |  | 2 |  |
| 1.3.3 | Subtraction | 2 |  |  |  | 2 |  |
| 1.3.4 | VAT calculation |  | 3 |  |  | 3 | Learners may find 14\% of R21,89 instead of subtracting |
| 1.4.1 | Read off table | 2 |  |  |  | 2 |  |
| 1.4.2 | Read off table | 2 |  |  |  | 2 |  |
| 1.4.3 | Read off table | 2 |  |  |  | 2 | Subtraction |
|  | TOTAL | 31 | 3 |  |  | 34 |  |

## Question 2

| 2.1.1 | Counting | 2 |  |  |  | 2 |  | Easy |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.1.2 | Probability | 2 |  |  |  | 2 |  |  |
| 2.1.3a | Circumference | 2 |  |  |  | 2 |  | Substitution in formula |
| 2.1.3b | Area of sector | 1 | 2 |  |  | 3 |  |  |
| 2.2.1 | Percentage increase | 1 | 2 |  |  | 3 |  | Is it necessary to give the formula? |
| 2.2.2 | Distance | 2 |  |  |  | 2 |  |  |
| 2.3.1 | Read off graph | 2 |  |  |  | 2 |  | 2 marks for reading-off a value |
| 2.3.2 | Read off graph | 1 |  |  |  | 1 |  | 1 mark for identifying who lives closer |
| 2.3.3 | Calculation of time | 2 |  |  |  | 2 |  |  |
| 2.3.4 | Estimation of arrival time | 2 |  |  |  | 2 |  |  |
| 2.3.5 | Interpretation from graph | 2 |  |  |  | 2 |  |  |
| 2.4.1 | Reading off table and then calculating |  | 3 |  |  | 3 |  | Not necessary to mention the R31,50 - it may just cause confusion |
| 2.4.2 | Substitution in formula | 3 |  |  |  | 3 |  |  |
|  | TOTAL | 22 | 7 |  |  | 29 |  |  |
| Question 3 |  |  |  |  |  |  |  |  |
| 3.1.1 | Hire purchase |  | 2 |  |  | 2 |  |  |
| 3.1.2 | Depreciation | 1 | 2 |  |  | 3 |  |  |
| 3.2.1 | Petrol consumption | 1 |  |  |  | 1 |  | Easy substitution |
| 3.2.2 | Petrol consumption | 2 |  |  |  | 2 |  |  |
| 3.3.1 | Grid reference | 2 |  |  |  | 2 |  |  |
| 3.3.2 | Read off street map | 2 |  |  |  | 2 |  |  |
| 3.3.3 | Direction |  | 2 |  |  | 2 |  | Will east be accepted? |
| 3.3.4 | Distance using a scale |  | 2 |  |  | 2 |  |  |
|  | TOTAL | 8 | 8 |  |  | 16 |  |  |
|  |  | 1 | 2 | 3 | 4 |  |  |  |
| Quest. | Content | Levels |  |  |  | Marks | Topic | Comment |

Association for Mathematics Education of South Africa

| Quest. | Content | Levels |  |  | Marks | Topic | Comment |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 |  |  |

Question 4

| 4.1.1 | Ascending order | 2 |  |  |  | 2 | Easy |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4.1.2 | Read from table | 1 | 1 |  |  | 2 | Subtraction |
| 4.1.3 | Mode of litter size | 2 |  |  |  | 2 | Use of the word "modal" may confuse learners |
| 4.1.4 | Range | 2 |  |  |  | 2 |  |
| 4.1.5 | Mean | 1 | 2 |  |  | 3 |  |
| 4.1.6 | Ratio | 1 | 1 |  |  | 2 |  |
| 4.1.7 | Compound bar graph |  | 7 |  |  | 7 | Half the graph is given; mark allocation too high |
| 4.2.1 | Length |  | 2 |  |  | 2 |  |
| 4.2.2 | Height - conversion | 2 |  |  |  | 2 | Easy multiplication |
|  | TOTAL | 11 | 13 |  |  | 24 |  |

## Question 5



Summary of marks and levels

| Question | Levels |  |  |  | Marks |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |  |
| 1 | 31 | 3 |  |  | 34 |
| 2 | 22 | 7 |  |  | 29 |
| 3 | 8 | 8 |  |  | 16 |
| 4 | 11 | 13 |  |  | 24 |
| 5 | 8 | 11 |  |  | 19 |
| 6 | 4 | 24 |  |  | 28 |
| Total | $\mathbf{8 4}$ | $\mathbf{6 6}$ |  |  | $\mathbf{1 5 0}$ |
| Percentage | $\mathbf{5 6 \%}$ | $\mathbf{4 4 \%}$ |  |  | $\mathbf{1 0 0} \%$ |

Association for Mathematics Education of South Africa

## MATHEMATICAL LITERACY PAPER 2

## A. OVERALL REVIEW

1. Technical Aspects (typing, diagrams, etc.)

The technical aspects of the paper are in keeping with the high standard set by the Department of Basic Education. However, question 1.1 (map-work), was difficult to work with as the intersection of national roads was not easy to pick up from the map.

## 2. Language used

This paper required a great deal of reading and interpretation. Although the language was mostly fair and within the scope of learners' reading ability, learners with a poor grasp of English would have struggled with the paper. However, learners who were taught well and were given enough practice with paper 2 type questions should have no problem with the language in the paper.
3. Syllabus coverage

| Code | Learning Outcomes | Suggested | November 2012 |
| :---: | :--- | :---: | :---: |
| LO1 | Numbers and operations in context | 37 | 39 |
| LO2 | Functional relationships | 38 | 34 |
| LO3 | Space, Shape and measurement | 38 | 41 |
| LO4 | Data Handling | 37 | 36 |
|  | Total | $\mathbf{1 5 0}$ | $\mathbf{1 5 0}$ |

The allocation of marks in the four learning outcomes was in according with the subject assessment guidelines as indicated in the above table. However, there teachers pointed out that key topics (contexts) such as compound interest, taxation and inflation were not included, while the horizontal bar graph and pie chart were included in both papers. Some teachers also questioned the relevance of the aircraft context in question 4.

### 4.1 Standard of paper

The paper was of a good standard as expected for Mathematical Literacy Paper 2. Learners had to do a lot of reading as the questions were very wordy. Learners may have had problems with the terminology used in the paper. In this regard, $2^{\text {nd }}$ language learners (with a poor grasp of English) would have been affected the most.
Teachers also stated that:

- Learners will struggle with the multi-step questions as very few guidelines were given.
- There are some cases where if learners can't get the first part of the question they will not be able to answer the rest of the question and will lose substantial marks
- In this regard, CA should be used in order for learners not to be unfairly penalized.

Teachers reported that, in general, learners struggled to complete the paper.

### 4.2 Compliance with levels of thinking

| Code | Levels of thinking | Suggested | November 2012 |
| :---: | :--- | :---: | :---: |
| 1 | Knowledge | $\pm 25 \%$ | - |
| 2 | Routine procedures | $\pm 30 \%$ | $20 \%$ |
| 3 | Complex procedures | $\pm 30 \%$ | $42 \%$ |
| 4 | Solving problems | $\pm 15 \%$ | $38 \%$ |

The cognitive levels in the paper as shown above are in keeping with the Subject Assessment Guidelines for Mathematical Literacy.

Association for Mathematics Education of South Africa
5. Comparison with 2011 paper

It was set along similar lines to the 2011 paper. There were a number of questions which required a great deal of reading and sifting through of information in a variety of guises (words, tables, graphs, pictures, diagrams). This made the paper very cognitively demanding and placed learners under added pressure.
6. Overall verdict

A very comprehensive paper set at the appropriate Grade 12 standard. The paper appeared to be balanced both cognitively and in terms of content coverage. We would classify this paper as being fair but challenging (in the context of what Mathematical Literacy Paper 2 is intended to achieve).

Although some key content/ contexts were not covered, teachers believed that this paper would more than compensate for the "easy" Paper 1.

## B. QUESTION BY QUESTION ANALYSIS:

| Quest. | Content | Levels |  |  | Marks | Topic | Comment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | 1 | 2 | 3 | 4 |  |  |

Question 1

| 1.1.1 | Direction | 2 |  |  | 2 | $\begin{aligned} & \hline \text { LO } 3 \\ & \text { LO1 } \\ & \text { LO2 } \end{aligned}$ | Fair |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.1.2 | Map-work | 2 |  |  | 2 |  | Too many routes to consider |
| 1.1.3 | Map-work - direction |  | 2 | 2 | 4 |  | Difficult to mark as it is not clear where national roads join |
| 1.2.1 | Payment | 2 |  |  | 2 |  | What is "nearly a week"? |
| 1.2.2a | Equation |  | 3 |  | 3 |  | Fair |
| 1.2.2b | Cost of meals | 2 | 2 |  | 4 |  | Confusing questions; contradictory |
| 1.2.3 | Financial |  |  | 9 | 9 |  | Confusing question; difficult to answer because of contradictory information |
|  | TOTAL | 8 | 7 | 11 | 26 |  |  |

Question 2

| 2.1.1.a | Measure of central tendency (time) |  | 2 |  |  | 2 | $\begin{gathered} \mathrm{LO} 3 \\ \text { LO4 } \end{gathered}$ | If they can't do this question they will lose marks in the next two parts of this question |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.1 .1 b | Use of mean calculation |  |  | 2 | 2 | 4 |  |  |
| 2.1.1 c | Median waiting |  |  | 3 |  | 3 |  |  |
| 2.1.2 | Application of lower quartile |  | 2 |  |  | 2 |  |  |
| 2.1.3 | Comparison with reasons |  |  |  | 4 | 4 |  | Too little marks allocated |
| 2.2.1 | Working with percentages |  |  | 2 | 2 | 4 |  | Ratio and proportion |
| 2.2.2 | Probability |  |  | 2 |  | 2 |  |  |
| 2.3.1 | Reasoning |  | 2 | 2 |  | 4 |  | Context may be foreign to some learners |
| 2.3.2 | Length |  |  |  | 9 | 9 |  | Difficult - formula for cylinder, not half cylinder being given, many steps. CA should apply to marking |
|  | TOTAL |  | 6 | 11 | 17 | 34 |  |  |
| Question 3 |  |  |  |  |  |  |  |  |
| 3.1.1 | Creating a formula |  | 2 |  |  | 2 | LO2 | Question 3 is a good question requiring insight |
| 3.1.2 a | Inverse proportion |  | 1 |  |  | 1 |  |  |
| 3.1.2 b | Calculation of missing values |  | 2 | 2 |  | 4 |  |  |
| 3.1.2 c | Drawing a graph |  |  | 4 |  | 4 |  |  |
| 3.2.1 | Increase in price |  |  | 2 |  | 2 |  | Possible reason |
| 3.2.2 | Disadvantage of increase in price |  |  | 2 |  | 2 |  |  |
| 3.2.3 | Drawing a graph |  | 4 | 4 |  | 8 |  | No table given |
| 3.2.4 | Calculation from graph |  |  | 3 |  | 3 |  |  |
|  | TOTAL |  | 9 | 17 |  | 26 |  |  |
|  |  | 1 | 2 | 3 | 4 |  |  |  |
| Quest. | Content | Levels |  |  |  | Marks | Topic | Comment |

Association for Mathematics Education of South Africa

| Quest. | Content | Levels |  |  |  | Marks | Topic | Comment |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 |  |  |  |
| Question 4 |  |  |  |  |  |  |  |  |
| 4.1.1 | Choosing from table |  |  | 3 |  | 3 | LO3 | Language " ... along with 37..." |
| 4.1.2 | Working out a scale |  |  | 4 |  | 4 |  |  |
| 4.1.3 | Distance |  |  | 3 |  | 3 |  | Too few marks |
| 4.1.4 | Making a choice after calculations |  |  |  | 4 | 4 |  | Reasoning and reflecting |
| 4.1.5 | Fuel capacity |  |  | 3 |  | 3 |  |  |
| 4.2.1 | Choosing from table |  |  |  | 3 | 3 |  | Very wordy; lots of reading and calculations for only 3 marks |
| 4.2.2 a | Drawing a line graph |  |  | 4 |  | 4 |  |  |
| 4.2 .2 b | Interpret line graphs |  |  |  | 3 | 3 |  | Reasoning |
|  | TOTAL |  |  | 17 | 10 |  |  |  |
| Question 5 |  |  |  |  |  |  |  |  |
| 5.1.1 | Read off from graph at correct place |  | 3 |  |  | 3 | $\begin{aligned} & \text { LO2 } \\ & \text { LO4 } \end{aligned}$ | Many learners will give answer only |
| 5.1.2 | Verifying calculations |  |  |  | 4 | 4 |  | The word "verify" may confuse learners; the word "determine" could have been used |
| 5.2.1 | Calculate missing values in table |  | 2 | 5 |  | 7 |  | Too many marks |
| 5.2.2 | Verifying calculations |  |  |  | 5 | 5 |  | See 5.1.2 |
| 5.2 .3 a | Calculation of bonus |  |  |  | 2 | 2 |  |  |
| 5.2 .3 b | Verification of Mabel's bonus |  |  |  | 8 | 8 |  |  |
| 5.3.1 | Interpreting compound bar graph |  |  | 2 |  | 2 |  |  |
| 5.3.2 | Interpretation of graph (errors) |  |  | 4 |  | 4 |  | Explaining errors in misinterpretation. |
| 5.3.3 | Naming other types of graphs |  | 2 |  |  | 2 |  |  |
|  | TOTAL |  | 7 | 11 | 19 | 37 |  |  |


| Summary of marks and levels |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Question | Levels |  | Marks |  |  |
|  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |  |
| $\mathbf{1}$ |  | 8 | 7 | 11 | 26 |
| 2 |  | 6 | 11 | 17 | 34 |
| 3 |  | 9 | 17 |  | 26 |
| 4 |  |  | 17 | 10 | 27 |
| 5 |  | 7 | 11 | 19 | 37 |
| Total | $\mathbf{0}$ | $\mathbf{3 0}$ | $\mathbf{6 3}$ | $\mathbf{5 7}$ | $\mathbf{1 5 0}$ |
| Percentage | $\mathbf{0 \%}$ | $\mathbf{2 0} \%$ | $\mathbf{4 2 \%}$ | $\mathbf{3 8} \%$ | $\mathbf{1 0 0} \%$ |

