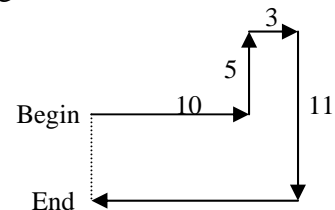


## NOTES ON MEMORANDUM

*These notes are necessarily brief and often formal and symbolic.*

**GRADE 4(1)**

1.  $(64 + 96) \div 2 = 80$
3.  $5 = \nabla - 8$ , so  $\nabla = 13$
4.  $72c \times 4 = R2,88$
5.  $3\heartsuit = \blacklozenge$ , so  $6\heartsuit = 2\blacklozenge$ , so  $X = 2\blacklozenge = 4\Delta$
6.  $102 \div 7 = 14$  and  $15 \times 7 = 105$ , so 3 more marbles are needed
7.  $6 \times 10$  or  $10 \times 6 = 60$
8.  $18 \times 10 = 180$
9. Make *equal parts*, e.g. 16 *triangles*, then 8 of 16 triangles =  $\frac{1}{2}$  of whole figure is shaded  
Or 8 *squares* with  $\frac{1}{2}$  of each square shaded, so  $\frac{1}{2}$  of whole figure is shaded
10. 6 small ones and 2 big ones for a total of 8
11.  $6 \times R0,75 - 2 \times R2 = 50c$
12. 08:00 – 70 min → 06:50
13. A rings on the hour and half-hour. B rings at 08:00, 08:35, 09:10, 09:45, 10:20, 10:55 and 11:30
14. If Mary has  $x$  stamps, Jason has  $2x$ , so  $x + 2x = 3x = 96$ , so  $x = 32$
15. Make a sketch:      **A ... 15 ... Stall ..... ? ..... B**      So  $15 + ? = 75$
16. The pattern is  $1 + \textcolor{blue}{1} + 1 + \textcolor{blue}{2} + 1 + \textcolor{blue}{3} + 1 + \textcolor{blue}{4} + 1 + [\textcolor{blue}{5} + 1 + \textcolor{blue}{6} + 1 + \textcolor{blue}{5}] + \textcolor{blue}{2} + 1 + \textcolor{blue}{8} + 1$ . So 18 in box!
17. Continue pattern of subtracting 4 cm/hour. Or the formula is: Height =  $32 - 4 \times \text{time}$
18.  $3 + 8 + 3 + 8 = 22$
19. Between  $\frac{1}{2}$  and  $\frac{3}{4}$  (i.e. about  $\frac{5}{8}$  of circle is shaded. So C.
20. Draw it physically, as shown to the right!
21. Imagine yourself positioned to the left behind the building and describe what you see ...
- 22.




96000			
160		600	
8	20	30	
2	4	5	6

23. For 6 milktarts she needs 8 cups of milk, so for 8 ( $6 + 2 = 6 + \frac{1}{3}$  of 6) milktarts she needs  $8 + \frac{1}{3}$  of 8 =  $8 + \frac{1}{3}$  of  $(6 + 2) = 8 + \frac{1}{3}$  of  $6 + \frac{1}{3}$  of 2 =  $8 + 2 + \frac{2}{3} = 10\frac{2}{3}$  cups of milk
24. With 15 eggs you can make the recipe  $1\frac{2}{3}$  times.  $6 \times 1\frac{2}{3} = 10$  milktarts
25. Be systematic, e.g.
- |    |    |    |    |
|----|----|----|----|
| 32 | 23 | 43 | 13 |
| 34 | 24 | 42 | 12 |
| 31 | 21 | 41 | 14 |

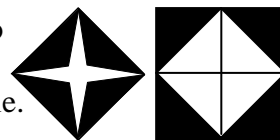
**GRADE 4(F)**

3. The watch gains 2 minutes every day for 7 days = 14 minutes
4.  $7 + 8 = 15$ . So Sizwe caught 7 fish
7. If Zuki has ♥ marbles, Zinkle has ♥ - 15. Together they have  $2 \times \heartsuit - 15 = 90$  marbles. So ♥ = 55
8.  $257 + \Delta = 438$ , so  $\Delta = 438 - 257 = 181$  km
9.  $438 + 169 = 607$  km
10. If 12 bottles cost R30, 4 bottles cost R10, and 8 bottles cost R20
12. Half of the previous number =  $1,7 \div 2 = 0,85$

13. 37 will be opposite 38, therefore Con lives opposite Luke
14. Delshe has  $71 + 24$ , Therine has  $71 - 24$ . In total they have  $71 + 24 + 71 - 24 = 71 \times 2 = 142$
15.  $R35,60 \div 40 = 0,89$ ;  $0,89 \times 15 = R13,35$
16.  $4 \times 3 \rightarrow 12 + 8 \rightarrow 20 \div 2 \rightarrow 10 - 6 \rightarrow 4$
17.  $\frac{3}{4} + \frac{3}{4} \rightarrow 1\frac{1}{2} + \frac{3}{4} \rightarrow 2\frac{1}{4} + \frac{3}{4} \rightarrow 3 + \frac{3}{4} \rightarrow 3\frac{3}{4} + \frac{3}{4} \rightarrow 4\frac{1}{2}$   
 ① ② ③ ④ ⑤ ⑥
18.  $2\frac{1}{5} + 2\frac{1}{5} + 2\frac{1}{5} + \dots$  15 times;  $15 \times 2 = 30$ ;  $15 \times \frac{1}{5} = 3$ ;  $30 + 3 = 33$
20. List all the possibilities and be systematic:  
 $1 + 1 = 2$     $2 + 2 = 4$     $3 + 3 = 6$     $4 + 4 = 8$     $5 + 5 = 10$     $6 + 6 = 12$   
 $1 + 2 = 3$     $2 + 3 = 5$     $3 + 4 = 7$     $4 + 5 = 9$     $5 + 6 = 11$   
 Any other combination will be a repetition – therefore 11 possible answers
21. Eby, Ram, Temba, Siva, Oscar – from tallest to shortest
22. 
23. Let the children be 1, 2, 3, 4 and 5. List all the possibilities and be systematic:  
 $1 \text{ vs } 2$     $2 \text{ vs } 3$     $3 \text{ vs } 4$     $4 \text{ vs } 5$   
 $1 \text{ vs } 3$     $2 \text{ vs } 4$     $3 \text{ vs } 5$   
 $1 \text{ vs } 4$     $2 \text{ vs } 5$   
 $1 \text{ vs } 5$
24. There are 36 tiles. 20 tiles are not covered (count halves).  $\frac{20}{36} = \frac{5}{9}$
25.  $1; 4; 9; 16; \dots = 1 \times 1; 2 \times 2; 3 \times 3; 4 \times 4; \dots$  So  $20 \times 20 = 400$

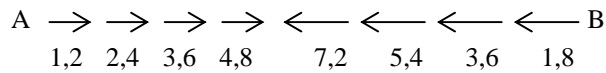
## **GRADE 5(1)**

1.  $11,23 < 11,32 < 11,4$  So Peter Davids is third
2. The watch gains  $4 \times 30 \text{ s} = 2$  minutes in one day, so 14 minutes in 7 days
4. B: Fold the black triangles into the white square ... they will fit exactly. So the black and white areas are equal, so the black area is  $\frac{1}{2}$  of the whole.  
 Or, if you see 4 squares, then  $\frac{1}{2}$  of each square is shaded, i.e.  $\frac{1}{2}$  of whole.  
 Or, cut the figure into equal triangles, then  $\frac{4}{8} = \frac{1}{2}$  triangles are shaded
5. It is not @, \*, # or X, so it is T
6. 12 chocolates weigh  $1,1 \text{ kg} - 680 \text{ g} = 420 \text{ g}$ , so 1 chocolate weighs  $420 \text{ g} \div 12 = 35 \text{ g}$   
 so 30 chocolates weigh  $30 \times 35 \text{ g} = 1050 \text{ g}$ , so box weighs  $1100 \text{ g} - 1050 \text{ g} = 50 \text{ g}$
7. Each number (except the first) is the previous number multiplied by 3
8. Test each of the given answers ... Or: If the number is N, then  $N - 1$  is divisible by 3, 5 and 6  
 The smallest number divisible by 6 is  $N - 1 = 3 \times 5 \times 2$  Why?? So  $N - 1 = 30$ , so  $N = 31$
9. Test each of the given answers ...  
 Or, find  $a$  (Susie's marbles) and  $b$  (Sam's) through trial and check so that  $a + b = 105$  and  $b - a = 25$   
 Or, if Sam has  $b$  marbles,  $(b - 25) + b = 105$ , so  $2 \times b - 25 = 105$ , so  $b = (105 + 25) \div 2 = 65$   
 Or, to do *equal* sharing, lend 25 marbles to Susie. Then, together they have  $105 + 25 = 130$ , so they each have  $130 \div 2 = 65$ . Now Susie must give back the extra 25 marbles we lent her!
11. Start numbering (painting) the sides ...
12. If their ages are  $a, b, c$  and  $d$ , then  $(a + 10) + (b + 10) + (c + 10) + (d + 10) = 100$ , so  $a + b + c + d = 60$
13. Draw equal triangles, then 4 out of 14 triangles are shaded
14. If  $C$  children like chocolate, then  $4 + 2 \times C = 40$ , so  $C = (40 - 4) \div 2 = 18$
15. If Joe's starting number is  $S$ , then he did  $S \times 10 = 9000$ . So  $S = 900$ . So correct answer is  $900 \div 10 = 90$
16. List them systematically:  
 $1, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19$   
 $21, 31, 41, 51, 61, 71, 81, 91$  and 100





21. man: 2 km after 30 min, 6 km after  $1\frac{1}{2}$  hours  
 wife: 0 km after 30 min, 6 km after  $1\frac{1}{2}$  hours
22. man walks 0,4 km every 6 min, wife walks 0,6 km every 6 min  
 man walks 1,2 km every 18 min, wife walks 1,8 km every 18 min



24.  $R11,50 \times 5 = R57,50$ ;  $R57,50 - R11,50 - R11,50 = R34,50$
25.  $1 + 2 + 3 + 4 + 5 + 6 + \dots + 47 + 48 + 49 + 50$   
 $= 51 + 51 + 51 + \dots$  25 times (compare no 19!)  
 $= 51 \times 25$   
 $= 1275$

### **GRADE 6(1)**

- $8 - 7,93 = 0,07 < 8,08 - 8 = 0,08$
- $1\Delta = 6\square$  and  $1\Delta + 1\odot = 10\square$ . So  $1\odot = 4\square$  and  $2\odot = 8\square$
- $\frac{13}{20}$  is more than  $\frac{12}{20}$  ( $\frac{3}{5}$ ) and less than  $\frac{16}{20}$  ( $\frac{4}{5}$ ), so he is on side DE
- He still has  $\frac{7}{20}$  of the distance to go, so  $\frac{7}{20}$  of 25 cm =  $(25 \text{ cm} \div 20) \times 7 = 8,75 \text{ cm}$
- The pattern is  $\div 6; \div 7; \div 8; \div 9; \dots$
- From the ground, over the length, to the ground again is  $6m + 8m + 6m = 20m$ , and from the ground, over the width, to the ground again is  $6m + 10m + 6m = 22m$
- Use trial and error ..., or:

$$\begin{aligned} \frac{3x+8}{2} - 6 &= x \\ \therefore 3x+8 &= 2(x+6) \\ \therefore x &= 4 \end{aligned}$$

- $17 + 18 + 19 = 54$ , so their product is  $17 \times 18 \times 19 = 5814$
- $\frac{8}{11} - \frac{5}{8} = \frac{9}{88}$  and  $\frac{9}{88} = 135 \text{ litres}$ , so  $\frac{1}{88} = 135 \div 9 = 15 \text{ litres}$ , so  $\frac{88}{88} = 15 \times 88 = 1320 \text{ litres}$
- 4 books = 2 books + 6 kg, so 2 books = 6 kg, so 1 book = 3 kg
- There is a general structure here: The denominators is twice the numerator + 1, i.e.  $\frac{\diamond}{2 \times \diamond + 1}$

We can therefore investigate a general pattern  $\frac{1}{3}, \frac{2}{5}, \frac{3}{7}, \frac{4}{9}, \frac{5}{11}, \frac{6}{13}, \frac{7}{15}, \dots$

Check with your calculator:  $\frac{1}{3} = 0,333\dots$ ,  $\frac{2}{5} = 0,4$ , ... So  $\frac{1}{3} < \frac{2}{5} < \frac{3}{7} < \frac{4}{9} < \frac{5}{11} < \frac{6}{13} < \frac{7}{15} < \dots$

Conclusion: the larger the denominator, the larger this kind of fraction, so  $\frac{11}{23}$  is the largest

- The gap will close at 8 mm/100 years. They have to grow 15 000 mm altogether. Therefore:

$$15\,000 \text{ mm} \div 8 \text{ mm/100 years} = 15\,000 \times \frac{100}{8} = 187\,500 \text{ years}$$

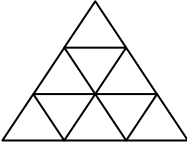
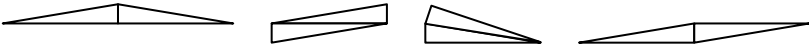
- Check all cases and note pattern:  $1 \times 17 = 17$ ;  $2 \times 16 = 32$ ;  $3 \times 15 = 45$ ;  $4 \times 14 = 56$ ; ...  $9 \times 9 = 81$
- Length =  $15 + 2 \times \text{Mass}$ , so Length (15) =  $15 + 2 \times 15 = 45$
- James is now  $2 \times 5 = 10$  years old, so 15 years from now he will be  $10 + 15 = 25$  years old.
- Make a systematic list, e.g. 3579; 3597 | 3759; 3795 | 3957; 3975 | 9375; 9357 | 9537 ...
- If the empty glass has a mass of  $g$  gram and milk  $m$  gram, then  $g + m = 370$  and  $g + \frac{1}{2}m = 290$ .

$$\text{So } \frac{1}{2}m = 370 - 290 = 80 \text{ grams, so } m = 160 \text{ grams and } g = 370 - 160 = 210 \text{ grams}$$

- $\frac{2002+2001}{2002-2001} = \frac{4003}{1} = 4003$

21. Let  $c$  be the cost of a coke and  $d$  the cost of a packet of chips. The cost of the first buy is  $6c + 7d$  and of the second is  $8c + 4d$ . So you bought 2 Cokes more, but 3 chips less, so 2 Cokes cost just as much as 3 packets of chips (compare the sentence  $6c + 7d = 8c + 4d$ ). So instead of  $8c + 4d = 4 \times 2c + 4d = 4 \times 3d + 4d = 12d + 4d = 16d$
22. Suppose he eats  $x$  bananas in the last hour, then  $(x + 15) + (x + 10) + (x + 5) + x = 90$   
So  $4x + 30 = 90$ , so  $x = 15$  bananas
23. There are 5 possible first digits (1, 3, 5, 7, 9) and 5 possible second digits, so in total  $5 \times 5 = 25$
24. Let the cost of eggs be  $R_e$ , chips  $R_c$ , etc.
- |   |    |  |
|---|----|--|
| $\begin{aligned} e + c &= R4,90 && \dots\dots\dots E_1 \\ s + c &= R6,00 && \dots\dots\dots E_2 \\ s + m &= R5,70 && \dots\dots\dots E_3 \\ E_1 - E_2: & e - s = -R1,10 && \dots\dots\dots E_4 \\ E_3 + E_4: & m + e = R4,60 \end{aligned}$ | or | $\begin{aligned} E_1 + E_2 + E_3: \\ e + 2s + 2c + m &= 16,60 \\ \therefore e + 2(s + c) + m &= 16,60 \\ \text{From } E_2: e + 2 \times 6 + m &= 16,60 \\ \therefore e + m &= R4,60 \end{aligned}$ |
|---|----|--|
25. For any two numbers  $a$  and  $b$ , the operation  $*$  is  $a * b = (a \times b) + (a + b)$

### **GRADE 6(F)**

1.  $365 \text{ days} \div 7 \text{ days/week} = 52 \text{ weeks and } 1 \text{ day} \dots$
- |                       |                       |
|-----------------------|-----------------------|
| 2003 Thu              | 2008 Thu (Leap year!) |
| 2004 Sat (Leap year!) | 2009 Fri              |
| 2005 Sun              | 2010 Sat              |
| 2006 Mon              | 2011 Sun              |
| 2007 Tue              | 2012 Tue (Leap year!) |
2.  $5,6 + 5,65 \rightarrow 11,25 \div 2 \rightarrow 5,625$
5.  $4653 - 2583 = 2070$ ;  $2070 \div 90 = 23$
- 6.
- 
8.  $\frac{5}{6} = \frac{40}{48}$  and  $\frac{7}{8} = \frac{42}{48} \therefore \frac{41}{48}$
9. From half to full in 1 minute  $\therefore 59$  minutes
11. About 8,6 in 1 hour ( $60 \div 7 = 8,57142$ )  
About 206 in 1 day ( $8,6 \times 24 = 206,4$ )  
About 75 000 in 1 year ( $206 \times 365 = 75190$ )
12.  $\frac{1}{2} + \frac{1}{8} + \frac{1}{8} = \frac{3}{4}$ ; R15 is  $\frac{1}{4}$ ; R60 =  $\frac{4}{4}$
13. If the book costs  $Rx$ , the CD costs  $Rx + 60$ . Together they cost  $x + x + 60 = 230$   
So  $x = (230 - 60) \div 2 = R85$
14. See Grade 4(1) number 11
15.  $43 = 8 \times 5 + 3$ ;  $78 = 10 \times 7 + 5 + 3$ ;  $56 = 8 \times 7$ ;  $47 = 6 \times 7 + 5$ . So all are possible
16. Jane eats 24 sweets in 5 minutes and 48 sweets in 10 minutes.
17.  $41 + 35 - 30 = 46$ ;  $50 - 46 = 4$
- 18.
- 
19. The tiger is the fastest, so A. The elephant is the heaviest, so C. The cat is the slowest and lightest, so E. The man is not as fast as the horse, and is lighter than the horse, so D is the man.
20.  $4 \times 1\frac{1}{2} = 6 \text{ cm}$ ;  $6 \times 1\frac{1}{2} = 9 \text{ cm}$

21. 11, 22, 33, 44, 55, 66, 77, 88, 99, (9)  
 101, 111, 121, 131, 141, 151, 161, 171, 181, 191, (10)  
 202, 212, 222, 232, 242, 252, 262, 272, 282, 292, (10)  
 303, etc. (10)  
 404, etc. (10)  
 So the total is 49

22. Make a table of the data, find a pattern and use the pattern to predict the answer:

Row number	Number of triangles
1	$1 = 2 \times 1 - 1$
2	$3 = 2 \times 2 - 1$
3	$5 = 2 \times 3 - 1$
4	$7 = 2 \times 4 - 1$
50	$2 \times 50 - 1 = 99$

23. Look systematically at special cases and find a pattern:

Total triangles in 1 row = 1

Total triangles in 2 rows =  $1 + 3 = 4 = 2^2$

Total triangles in 3 rows =  $1 + 3 + 5 = 9 = 3^2$

Total triangles in 4 rows =  $1 + 3 + 5 + 7 = 16 = 4^2$

So, total triangles in 50 rows =  $50^2 = 50 \times 50 = 2\,500$

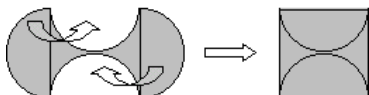
24. It really is the same question as 23 – the numbers and the number of triangles are the same!

So  $15^2 = 15 \times 15 = 225$

25. The pattern is  $1 \times 2, 2 \times 3, 3 \times 4, 4 \times 5, \dots$  So  $50 \times 51 = 2550$

### GRADE 7(1)

1. E:  $4 + 4 - 4 \div 4 = 8 - 1 = 7 \neq 1$

2.  So  $6 \text{ cm} \times 6 \text{ cm} = 36 \text{ cm}^2$

4. 

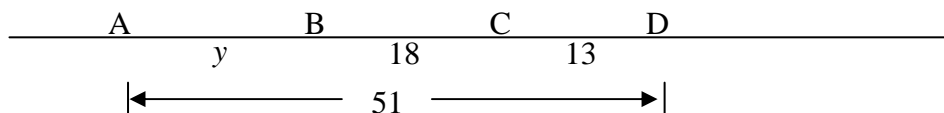
6. 10 out of 100 pears are not sold. So 550 out of 5500 are not sold

7. The Fibonacci sequence: Each number (except the first two) is the sum of the previous two

10. The idea is *not* to read off values, but to interpret the *form* of the graph – where is it increasing, decreasing, or where does it reach a maximum, etc.

11. First find the buying price  $x$ :  $1,3 \times x = \text{R}78$ , so  $x = \text{R}60$ . To make 60% profit:  $\text{R}60 \times 1,6 = \text{R}96$

12. Make a sketch of the towns and fill in the known details:



$$x = BD = 18 + 13$$

$$13. y = AB = 51 - (18 + 13)$$

14. Area =  $20 \text{ cm} \times 10 \text{ cm} = 200 \text{ cm}^2$ . So  $16 \times w = 200$ , so  $w = 200 \div 16 = 12,5 \text{ cm}$  i.e. 2,5 cm *longer*

15. Make sketches to understand the structure:  $144 \text{ cm}^2 = 12 \text{ cm} \times 12 \text{ cm}$ , so there will be 13 dots along each side. But the dots on the corners are counted twice, so  $13 \times 4 - 4 = 48$  dots

16. 

17.  $\frac{1}{13} < \frac{5}{61} < \frac{1}{n} < \frac{13}{57} < \frac{1}{4}$ , i.e.  $\frac{1}{13} < \frac{1}{n} < \frac{1}{4}$ , so  $n$  can be 12, 11, 10, 9, 8, 7, 6 and 5.
18. If  $x$  is the price without VAT, then  $1,14 \times x = 9,46$ . So  $x = R8,30$ , so VAT = R1,16
19. Let Lynn weigh  $L$  kg etc. Add everything together:  $2L + 2F + 2S = 420$ , so  $L + F + S = 210$   
But  $L + F = 132$ , so  $(L + F) + S = 210$ , i.e.  $132 + S = 210$ , so  $S = 78$  kg
20. It is a base 5 system:  
 $\text{***}$  for  $7 = 5 + 2$   
 $\text{***}$  for  $28 = 25 + 3 = 5^2 + 3$   
 $\text{***}$  for  $62 = 50 + 10 + 2 = 2 \times 5^2 + 2 \times 5 + 2$   
 So  $91 = 75 + 15 + 1 = 3 \times 5^2 + 3 \times 5 + 1 = \text{***}$
21. If the youngest sister has  $Rx$ , then we can represent the situation symbolically by:  
 $x + (x + 2) + (x + 4) + (x + 6) + (x + 8) = 100$ , so  $5 \times x + 20 = 100$   
 Or think of it like this: to make an equal sharing situation, first take away the extra money they get ( $2 + 4 + 6 + 8 = R20$ ). Then there is R80 to be shared equally between the 5 sisters – each receives R16. Then give them the R2, R4, etc. that they get more than the younger sister
22. If the numbers are  $x_1, x_2, \dots$  then  $x_1 + x_2 + \dots + x_7 = 7 \times 49$   
 $\therefore (x_1 + 1) + (x_2 + 2) + \dots + (x_7 + 7) = (x_1 + x_2 + \dots + x_7) + (1 + 2 + \dots + 7) = 7 \times 49 + 4 \times 7$   
 To get the new average, divide by 7:  $(7 \times 49 + 4 \times 7) \div 7 = 49 + 4 = 53$
23. Make an appropriate representation, e.g. take the special case of 4 teams, A, B, C and D:

vs	A	B	C	D
A		X	X	X
B			X	X
C				X
D				

So 12 teams plays a total of  $11 + 10 + 9 + \dots + 3 + 2 + 1 = 66$  games (do you have a short method?)

24. The time they run is equal, and time = distance  $\div$  speed  
 Suppose the distance run by the cat is  $x$  metres, then the distance the dog runs is  $x + 36$  metres  

$$\frac{x+36}{7} = \frac{x}{5}$$

$$\therefore x = 90$$

Can you find a more informal explanation?

25. If 60% die, then 40% of trees are alive after first year  
 After 2 years, 40% of 40% =  $0,4 \times 0,4 = 0,16 = 16\%$  of trees are alive  
 After 3 years, 40% of 16% =  $0,4 \times 0,16 = 0,064 = 6,4\%$  of trees are alive

## **GRADE 7(F)**

- $3 \times 5 + 2 \times 6 - 1 \times 2$  (the overlap) =  $23 \text{ cm}^2$
- $3 + 3 + 5 + 2 + 4 + 2 + 6 + 1 = 26 \text{ cm}$
- $180 \div 5 \times 9 = 67,5 \text{ g}$
- $530,20 \times 0,2 \text{ g} = 106,04 \text{ g}$
- Write the product of factors, but do not repeat factors, e.g. do not write  $6 = 2 \times 3$ , because it is already there!
- Use the fact that the diagonal of a rectangle halves the area of the rectangle.
- $(2 + 4 + 6 + 8 + \dots + 98 + 100) - (1 + 3 + 5 + \dots + 97 + 99)$   
 $= (2 - 1) + (4 - 3) + (6 - 5) + \dots + (98 - 97) + (100 - 99)$   
 $= 1 + 1 + 1 + 1 + \dots$  50 times = 50
- If Sandy is  $x$  years old, Mandy is  $x + 7$  years old. In 4 years time Sandy is  $x + 4$  years old and Mandy is  $x + 11$ . Then  $x + 4 = \frac{1}{2} \times (x + 11)$ . So  $x$ , i.e. Sandy is 3 and Mandy is 10.  $3 + 10 = 13$

11. 20, 22, 24, 26, 28, (5)  
 40, 42, 44, 46, 48, (5)  
 60, 62, 64, 66, 68, (5)  
 80, 82, 84, 86, 88 (5) So the total is 20
12.  $2^2 + 9^2 = 4 + 81 = 85$   
 $6^2 + 7^2 = 36 + 49 = 85$
13. 12:9. So 3 revolutions will be 36 clicks, which will revolve B 4 times.
14. Test all the cases systematically:  $1 \times 17 = 17$ ;  $2 \times 16 = 32$ ;  $3 \times 15 = 45$ ; ...  $9 \times 9 = 81$ , then the answer repeats, because the order does not matter (e.g.  $2 \times 16 = 16 \times 2$ ).
15. 1, 2, 4, 5, 8, 10, 16, 20, 25, 80, 40, 50, 100, 125, 200, 250, 400, 500, 1000, 2000

16. 

		<b>Z</b>
11	6	<b>A</b>
		10

  
 $11 + 6 + A = 18$ , so  $A = 1$   
 $Z + A + 10 = 18$ , so  $Z = 7$

17. Be systematic!  
 $9 + 9 + 7 = 25$   
 $9 + 8 + 8 = 25$   
 $9 + 7 + 9 = 25$   
 $8 + 9 + 8 = 25$   
 $8 + 8 + 9 = 25$   
 $7 + 9 + 9 = 25$
18. You can draw it, or investigate numerical patterns for a triangle, square, pentagon, hexagon, etc. Or you can reason it out: At each vertex of an  $n$ -gon there are  $n - 3$  diagonals (the point is connected to every other point, except to the two adjacent points and itself). So at  $n$  vertices there are  $n \times (n - 3)$  diagonals. But do not count the diagonals twice! So  $n \times (n - 3) \div 2$ .  
 So if  $n = 8$ , the number of diagonals is  $8 \times 5 \div 2 = 20$
19. We know: Sum of numbers  $\div 11 = 8$ , so the sum is 88  
 If the new number is  $x$ , then  $(88 + x) \div 12 = 11$ . So  $x = 12 \times 11 - 88 = 44$
20. If there were  $x$  tests before the last, his total marks were  $62 \times x$ .  
 After the last test,  $\frac{62 \times x + 70}{x + 1} = 64$ , so  $x = 4$ .
21. Perimeter  $= 2l + 2b = 12$ , so  $l + b = 6$ . But it is a *square*, so  $l = b = 3$ . So Area  $= 3 \text{ m} \times 3 \text{ m} = 9 \text{ m}^2$
22. Look for structure!  $T_{50} = 1 + 2 + 3 + 4 + \dots + 49 + 50 = 25 \times 51 = 1275$
23. Look for structure and pattern!

$$N_1 = 1$$

$$N_2 = 5 = 2^2 + 1$$

$$N_3 = 10 = 3^2 + 1$$

$$N_4 = 17 = 4^2 + 1$$

Test the numbers!  $30^2 + 1 = 901$  is the only one which fits the pattern.

24. If they mine 5%, then 95% = 0,95 is left. So:  
 After 1 year, 95% is left  
 After 2 years, 95% of 95% =  $0,95 \times 0,95$  is left  
 After 3 years, 95% of 95% of 95% =  $0,95 \times 0,95 \times 0,95 = 0,95^3$  is left  
 After 10 years,  $0,95^{10}$  is left. Use a calculator:  $0,95^{10} = 0,598 = 59,8\%$  is left  
 After 13 years,  $0,95^{13}$  is left.  $0,95^{13} = 0,513 = 51,3\%$ , more than half, is left  
 After 14 years,  $0,95^{14}$  is left.  $0,95^{14} = 0,487 = 48,7\%$ , less than half, is left

$$\begin{aligned} 25. (1 + 1) \times (1 + \frac{1}{2}) \times \dots &= \frac{2}{1} \times \frac{3}{2} \times \frac{4}{3} \times \frac{5}{4} \times \dots \times \frac{100}{99} \times \frac{101}{100} \\ &= \frac{2}{2} \times \frac{3}{3} \times \frac{4}{4} \times \frac{5}{5} \times \dots \times \frac{100}{100} \times \frac{101}{1} \\ &= 101 \end{aligned}$$