

SA Mathematics Challenge 2013

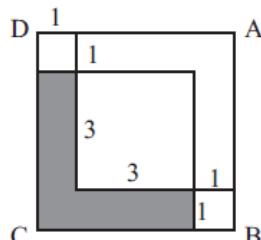
GRADE 7 FINAL ROUND

4 SEPTEMBER 2013

NOTE:

- Answer the questions according to the instructions on the answer sheet.
- You may use a calculator.
- The questions test insight. Complex calculations will therefore not be necessary.
- We hope you enjoy it!

1. Figure ABCD is a square. Inside this square three smaller squares are drawn with side lengths (in centimetres) as labelled. What is the area of the shaded L-region?



- (A) 7 cm^2 (B) 10 cm^2 (C) $12,5 \text{ cm}^2$ (D) 14 cm^2 (E) 15 cm^2

2. What is the perimeter of the shaded L-region in question 1?

- (A) 14 cm (B) 10 cm (C) 12 cm

3. Calculate:

$$2 - 1 + 3 - 2 + 4 - 3 + 5 - 4 + 6 - 5 + \dots + 101 - 100$$

- (A) 99 (B) 100 (C) 101

4. The number 64 has the property that it is divisible by its units digit (4). How many whole numbers between 10 and 50 have this property?

- (A) 15 (B) 16 (C) 17

5. What is the 83rd number in the following pattern?

$$1; 3; 5; 7; \dots$$

- (A) 85 (B) 165 (C) 62

SA Wiskunde-uitdaging 2013

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LET OP:

- Beantwoord die vrae volgens die instruksies op die antwoordblad.
- Jy mag 'n sakrekenaar gebruik.
- Die vrae toets insig. Omslagtige berekeninge is dus onnodig en tydwend.
- Ons hoop jy geniet dit!

1. Figuur ABCD is 'n vierkant. Drie kleiner vierkante word getrek met sylengtes (in sentimeter) soos getoon. Wat is die oppervlakte van die verdonkerde L-gebied?

2. Wat is die omtrek van die verdonkerde L-gebied in vraag 1?

- (D) 16 cm (E) None of these
Nie een hiervan nie

3. Bereken:

$$2 - 1 + 3 - 2 + 4 - 3 + 5 - 4 + 6 - 5 + \dots + 101 - 100$$

- (D) 102 (E) None of these
Nie een hiervan nie

4. Die getal 64 het die eienskap dat dit deelbaar is deur sy ene-syfer (4). Hoeveel heelgetalle tussen 10 en 50 het hierdie eienskap?

- (D) 18 (E) 20

5. Wat is die 83^{ste} getal in die volgende patroon?

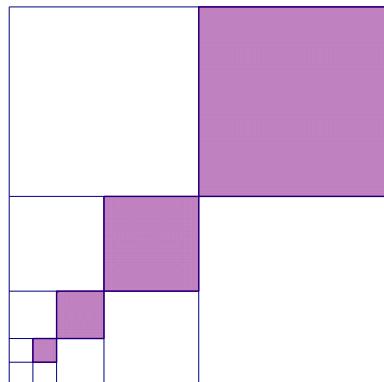
$$1; 3; 5; 7; \dots$$

- (D) 97 (E) 102

13. There are three children in a certain family. What is the probability that at least one of the three children is a girl?

(A) $\frac{1}{2}$ (B) $\frac{1}{3}$ (C) $\frac{1}{8}$ (D) $\frac{3}{8}$ (E) $\frac{7}{8}$

14. A square is divided into four smaller equal squares, and the process is then repeated as shown. What fraction of the large square is shaded?



(A) $\frac{1}{4}$ (B) $\frac{17}{64}$ (C) $\frac{85}{256}$ (D) $\frac{7}{16}$ (E) $\frac{65}{128}$

15. How many of the 5-digit numbers which consist of the five digits 1, 2, 3, 4 and 5 are divisible by all of 1, 2, 3, 4 and 5?

(A) 0 (B) 1 (C) 18 (D) 24 (E) 120

16. Find the number between 20 and 80 which meets all the following conditions:

it is a prime number

if you reverse its digits, this new number is also prime
if you add 1 to the number you get a multiple of 3

(A) 53 (B) 31 (C) 67 (D) 71 (E) None of these
Nie een hiervan nie

17. What is the smallest number that is divisible by 1, 2, 3, 4, 5, 6, 7, 8, 9 and 10?

(A) $3 \times 4 \times 5 \times 7 \times 9$ (B) $5 \times 7 \times 8 \times 9$ (C) $5 \times 6 \times 7 \times 8 \times 9$ (D) $5 \times 6 \times 8 \times 9$ (E) $2 \times 3 \times 4 \times 5 \times 6 \times 7 \times 8 \times 9 \times 10$

18. Excluding 1 and itself, how many factors does the number $19 \times 29 \times 59 \times 79$ have?

(A) 4 (B) 8 (C) 10 (D) 12 (E) 14

19. A painter takes two days to paint a room (all four walls and the ceiling). If he works at the same pace, how many days will he take to paint a room that is twice as wide, twice as long and twice as high?

(A) 2 (B) 4 (C) 5 (D) 6 (E) 8

13. 'n Familie het drie kinders. Wat is die waarskynlikheid dat minstens een van die drie kinders 'n meisie is?

(A) $\frac{1}{2}$ (B) $\frac{1}{3}$ (C) $\frac{1}{8}$ (D) $\frac{3}{8}$ (E) $\frac{7}{8}$

14. 'n Vierkant word in vier ewe-groot kleiner vierkante verdeel, en die proses word dan herhaal soos getoon. Watter breuk van die groot vierkant is verdonker?

15. Hoeveel van die 5-syfer getalle wat bestaan uit die vyf syfers 1, 2, 3, 4 en 5 is deelbaar deur 1 en 2 en 3 en 4 en 5?

(D) 24

16. Vind die getal tussen 20 en 80 wat aan al die volgende voorwaardes voldoen:

dit is 'n priemgetal

as jy die syfers omruil, is die nuwe getal ook priem
as jy 1 by die getal tel kry jy 'n veelvoud van 3

(D) 71 (E) None of these
Nie een hiervan nie

17. Wat is die kleinste getal wat deelbaar is deur 1, 2, 3, 4, 5, 6, 7, 8, 9 en 10?

(D) $5 \times 6 \times 8 \times 9$ (E) $2 \times 3 \times 4 \times 5 \times 6 \times 7 \times 8 \times 9 \times 10$

18. Behalwe 1 en die getal self, hoeveel faktore het die getal $19 \times 29 \times 59 \times 79$?

(D) 12 (E) 14

19. 'n Verwer neem twee dae om 'n kamer te verf (al vier mure en die plafon). As hy teen dieselfde tempo werk, hoeveel dae sal hy verf aan 'n kamer twee keer so lank, twee keer so breed en twee keer so hoog?

(D) 6 (E) 8

20. Arnie, Bender and Cross are three robots. They are weighed two at a time. Here are the results:

$$A + B = 12 \text{ kg} \quad B + C = 14 \text{ kg} \quad C + A = 16 \text{ kg}$$

How much will all three weigh together?

- (A) 21 kg (B) 42 kg (C) 28 kg

20. Armie, Bender en Cross is drie robotte. Hulle word twee op 'n slag geweeg. Hier is die lesings:

$$A + B = 12 \text{ kg} \quad B + C = 14 \text{ kg} \quad C + A = 16 \text{ kg}$$

Hoeveel sal al drie saam weeg?

- (D) 32 kg (E) 14 kg

21. In the previous question, how much does Bender weigh on its own?

- (A) 5 kg (B) 6 kg (C) 7 kg

21. In die vorige vraag, hoeveel weeg Bender op sy eie?

- (D) 8 kg (E) 9 kg

22. Calculate:

$$\frac{1+3+5+7+\dots+97+99}{2+4+6+8+\dots+98+100}$$

- (A) $\frac{50}{51}$ (B) $\frac{99}{100}$ (C) $\frac{49}{50}$

22. Bereken:

$$\frac{1+3+5+7+\dots+97+99}{2+4+6+8+\dots+98+100}$$

- (D) $\frac{1}{2}$ (E) None of these
Nie een hiervan nie

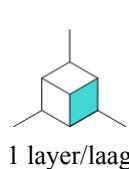
23. Xolile has a bag of marbles. He gave $\frac{1}{3}$ of them to Baba and then $\frac{1}{4}$ of the remaining marbles to Sam. If there are now 24 marbles in the bag, how many marbles did Xolile give to Baba?

- (A) 8 (B) 16 (C) 48

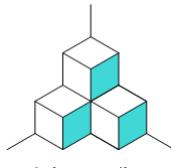
23. Xolile het 'n sak albasters. Hy gee $\frac{1}{3}$ van hulle aan Baba en gee toe $\frac{1}{4}$ van die oorblywende albasters aan Sam. As daar nou 24 albasters in die sak is, hoeveel albasters het Xolile aan Baba gegee?

- (D) 24 (E) None of these
Nie een hiervan nie

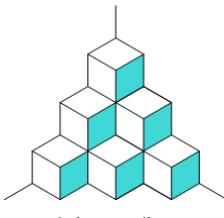
24. Blocks are stacked in the corner of a room as illustrated. How many blocks are used if they are stacked to 6 layers?



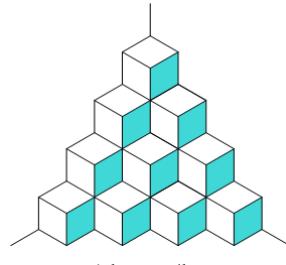
1 layer/laag



2 layers/lae



3 layers/lae

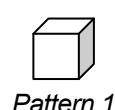


4 layers/lae

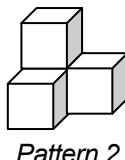
- (A) 35 (B) 56 (C) 36 (D) 45 (E) 21

24. Blokkies word in die hoek van 'n kamer gestapel soos getoon. Hoeveel blokkies sal daar in 'n stapel met 6 lae wees?

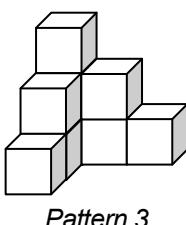
25. Siphokazi builds a pattern of cubes as shown. How many cubes will there be in *Pattern 20*?



Pattern 1



Pattern 2



Pattern 3

- (A) 312 (B) 400 (C) 412 (D) 441 (E) 40

25. Siphokazi bou patronne met kubusse soos getoon. Hoeveel kubusse sal in *Patroon 20* wees?